

Calculus Lesson 133 One Sided Limits

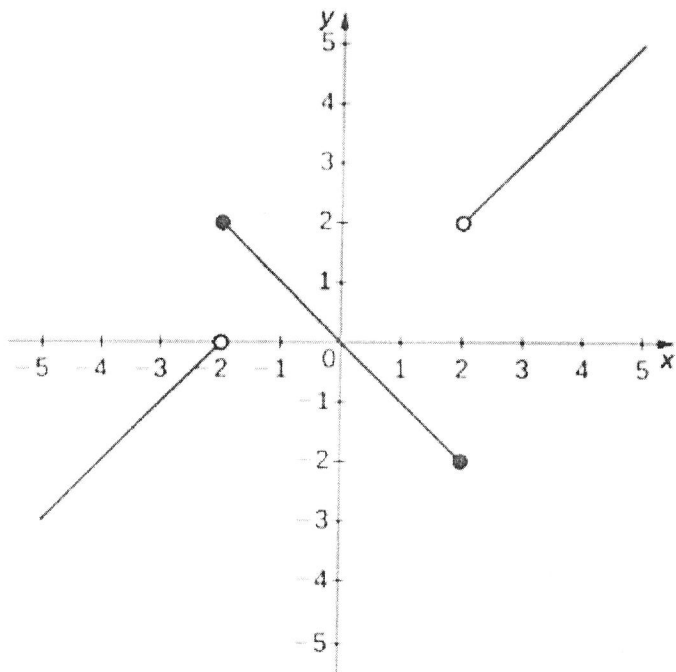
One Sided Limits

If you only want to know what y-value a function approaches as the x-value moves toward 3

(or any other value) from the LEFT, you will see $\lim_{x \rightarrow 3^-} f(x) =$

If you only want to know what y-value a function approaches as the x-value moves toward 3

(or any other value) from the RIGHT, you will see $\lim_{x \rightarrow 3^+} f(x) =$



59. $\lim_{x \rightarrow -2^-} f(x)$

60. $\lim_{x \rightarrow -2^+} f(x)$

61. $\lim_{x \rightarrow -2} f(x)$

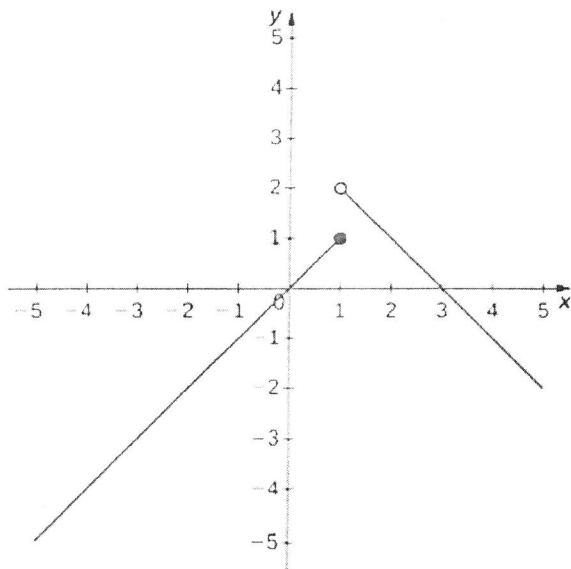
62. $\lim_{x \rightarrow 2^-} f(x)$

63. $\lim_{x \rightarrow 2^+} f(x)$

64. $\lim_{x \rightarrow 2} f(x)$

HW: complete worksheet 133

In the following exercises, use the following graph of the function $y = f(x)$ to find the values, if possible. Estimate when necessary.



50. $\lim_{x \rightarrow 1^-} f(x)$

51. $\lim_{x \rightarrow 1^+} f(x)$

52. $\lim_{x \rightarrow 1} f(x)$

53. $\lim_{x \rightarrow 2} f(x)$

54. $f(1)$

In Exercises 7–24, find the limit (if it exists). If it does not exist, explain why.

7. $\lim_{x \rightarrow 5^+} \frac{x-5}{x^2-25}$

8. $\lim_{x \rightarrow 2^+} \frac{2-x}{x^2-4}$

9. $\lim_{x \rightarrow 3^-} \frac{x}{\sqrt{x^2-9}}$

10. $\lim_{x \rightarrow 4^+} \frac{\sqrt{x}-2}{x-4}$

11. $\lim_{x \rightarrow 0} \frac{|x|}{x}$

12. $\lim_{x \rightarrow 2^+} \frac{|x-2|}{x-2}$

13. $\lim_{\Delta x \rightarrow 0^+} \frac{\frac{1}{x+\Delta x} - \frac{1}{x}}{\Delta x}$

14. $\lim_{\Delta x \rightarrow 0^+} \frac{(x+\Delta x)^2 + x + \Delta x - (x^2 + x)}{\Delta x}$

103. $\lim_{x \rightarrow -2^-} \frac{2x^2 + 7x - 4}{x^2 + x - 2}$

104. $\lim_{x \rightarrow -2^+} \frac{2x^2 + 7x - 4}{x^2 + x - 2}$

105. $\lim_{x \rightarrow 1^-} \frac{2x^2 + 7x - 4}{x^2 + x - 2}$

106. $\lim_{x \rightarrow 1^+} \frac{2x^2 + 7x - 4}{x^2 + x - 2}$

Review:

15. If $f(x) = \frac{x^2 + 5x - 24}{x^2 + 10x + 16}$, then $\lim_{x \rightarrow -8} f(x)$ is

- (A) 0 (B) 1 (C) $-\frac{3}{2}$ (D) $\frac{11}{6}$ (E) Nonexistent

24. $\lim_{x \rightarrow 0} \frac{\tan(3x) + 3x}{\sin(5x)} =$

- (A) 0 (B) $\frac{3}{5}$ (C) 1 (D) $\frac{6}{5}$ (E) Nonexistent

31. $\lim_{h \rightarrow 0} \frac{\tan\left(\frac{\pi}{6} + h\right) - \tan\left(\frac{\pi}{6}\right)}{h} =$

- (A) $\frac{\sqrt{3}}{3}$ (B) $\frac{4}{3}$ (C) $\sqrt{3}$ (D) 0 (E) $\frac{3}{4}$

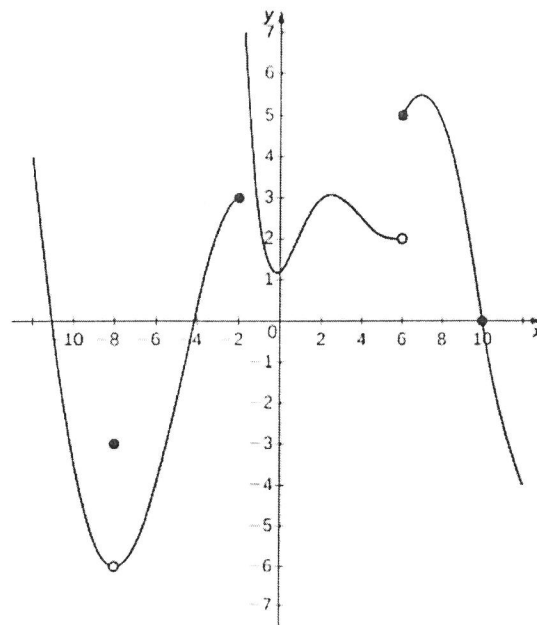
For the following exercises, consider the function $f(x) = (1 + x)^{1/x}$.

32. [T] Make a table showing the values of f for $x = -0.01, -0.001, -0.0001, -0.00001$ and for $x = 0.01, 0.001, 0.0001, 0.00001$. Round your solutions to five decimal places.

| x | $f(x)$ | x | $f(x)$ |
|----------|--------|---------|--------|
| -0.01 | a. | 0.01 | e. |
| -0.001 | b. | 0.001 | f. |
| -0.0001 | c. | 0.0001 | g. |
| -0.00001 | d. | 0.00001 | h. |

33. What does the table of values in the preceding exercise indicate about the function $f(x) = (1 + x)^{1/x}$?

34. To which mathematical constant does the limit in the preceding exercise appear to be getting closer?



46. $\lim_{x \rightarrow 10^-} f(x) = 0$

47. $\lim_{x \rightarrow -2^+} f(x) = 3$

48. $\lim_{x \rightarrow -8^-} f(x) = f(-8)$

49. $\lim_{x \rightarrow 6^-} f(x) = 5$